



VIBRANT MEscope Application Note 44

Structural Dynamics Modification (SDM)

The steps in this Application Note can be carried out using any MEscope package that includes the **VES-5000 SDM option**. Without this option, you can still carry out the steps in this App Note using the **AppNote44** project file. These steps might also require MEscope software with a *more recent release date*.

APP NOTE 44 PROJECT FILE

- To retrieve the Project for this App Note, [click here](#) to download **AppNote44.zip**

This Project contains *numbered Hotkeys & Scripts* for carrying out the steps of this App Note.

- *Hold down the Ctrl key and click on a Hotkey* to open its Script window

IN THIS APP NOTE

This App Note contains two examples that illustrate uses of **SDM**,

- Adding an **axial stiffener** between the top & bottom plates of the Jim Beam structure
- Adding a **3-DOF stiffener** between the top & bottom plates of the Jim Beam

MODELING STRUCTURAL DYNAMIC MODIFICATIONS

There are only two ways to *reduce vibration levels* in a machine or structure,

1. *Isolate* the structure from its excitation forces
2. *Physically modify* the structure or *change its boundary conditions*

The vibration of a machine or structure will change if,

1. A *physical property* (mass, stiffness, or damping) is changed
2. A *boundary condition* is changed
3. Two or more structural components *are coupled together*

SDM AND THE LAW OF MODAL ANALYSIS

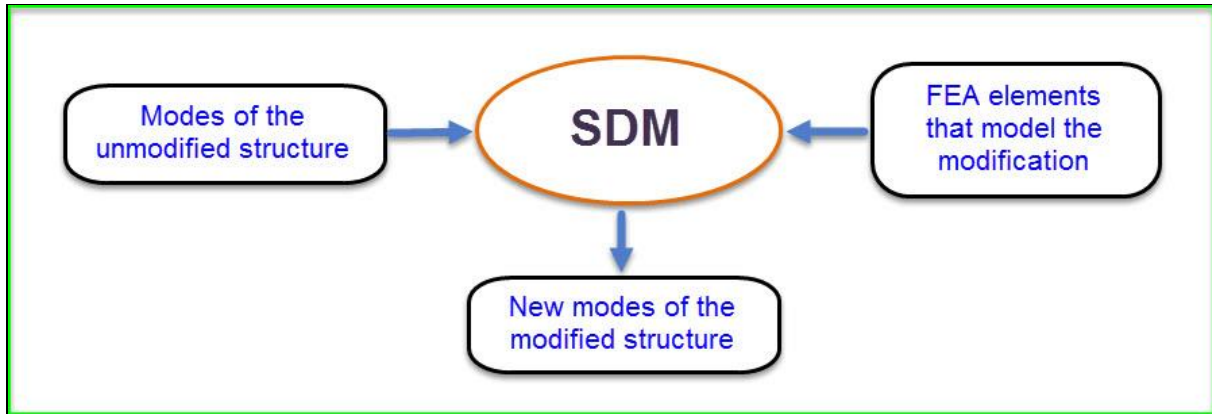
SDM relies on a **Law of Modal Analysis** to perform its calculations. It uses a **Modal Model** of the *unmodified structure* together with FEA Objects that define the structural modifications to calculate the mode shapes of the *modified structure*.

Law of Modal Analysis: *All vibration is a summation of mode shapes.*

The **Structural Dynamics Modification (SDM)** method allows you to model one of the three types of modifications, **physical change**, **boundary condition change**, or **component coupling (sub-structuring)**. **SDM** calculates the new modal parameters (**frequency, damping, & mode shape**) that result from making those structural modifications.

SDM converts all structural modifications into **changes in the mass, stiffness & damping properties** of the structure. Those mass, stiffness, & damping changes are used together with the **mode shapes of the unmodified structure** to calculate the **new modes of the modified structure**.

SDM calculates the mode shapes of the *modified structure* as **weighted summation of the mode shapes** of the *unmodified structure*, therefore utilizing of the **Law of Modal Analysis**.



MODAL MODEL

SDM is unique in that it works directly with a **Modal Model** of the *unmodified structure*. The **Modal Model** can contain mode shapes from an **Experimental Modal Analysis** called **EMA mode shapes**, mode shapes from a **Finite Element Analysis** called **FEA mode shapes**, or both **EMA & FEA modal parameters merged together** in a **Hybrid Modal Model**.

A **Modal Model** is a set of **scaled mode shapes**.

SDM requires the mode shapes to be scaled to Unit Modal Masses, called UMM mode shapes

A **Modal Model** preserves the dynamic properties of a structure (its mass, stiffness & damping properties), and therefore can be used to **fully represent Input Output structural dynamics**.

Once the dynamic properties of an *unmodified structure* are defined in terms of its **Modal Model**, **SDM** can be used to predict the dynamic effects of modifications to the structure. These modifications can be as simple as **additions or removals of point masses, linear springs, or linear dampers**. Or more complex structural modifications can be modeled using **FEA elements** such **rods & bars, plates (membranes) and solid elements**.

SDM is computationally very efficient because it solves an eigenvalue problem in **modal space**. The eigenvalue problem size is determined by the number of modes in the **Modal Model**.

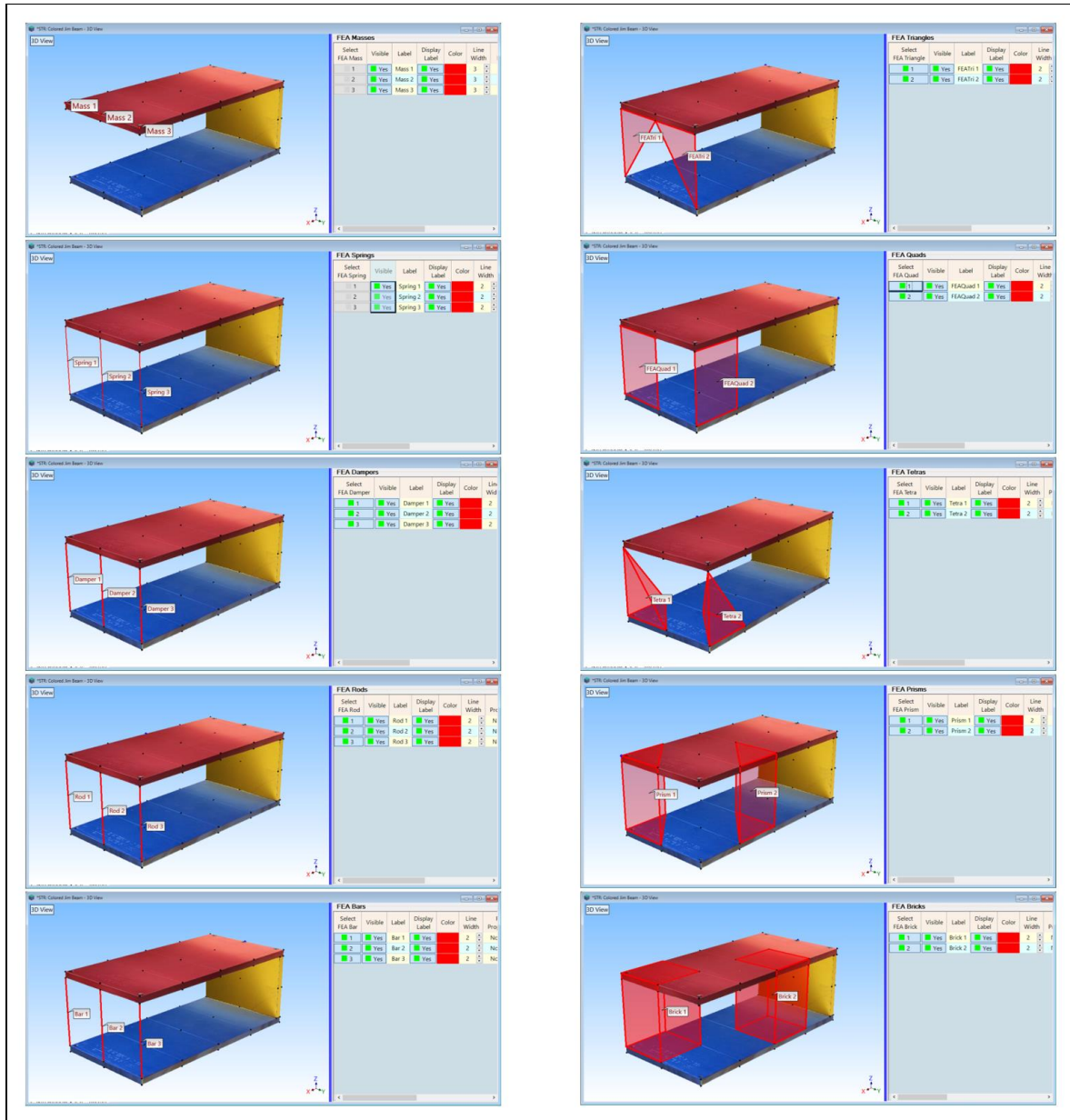
Another advantage of **SDM** is that the **Modal Model** of the *unmodified structure* must only contain mode shape data for the **DOFs (points & directions) where the modification elements are attached** to the structure.

FEA OBJECTS FOR MODELING STRUCTURAL MODIFICATIONS

SDM uses **industry-standard finite elements** to model structural modifications.

Finite elements are called **FEA Objects** in MEScope.

The following types of **FEA Objects** can be used for modeling structural modifications.

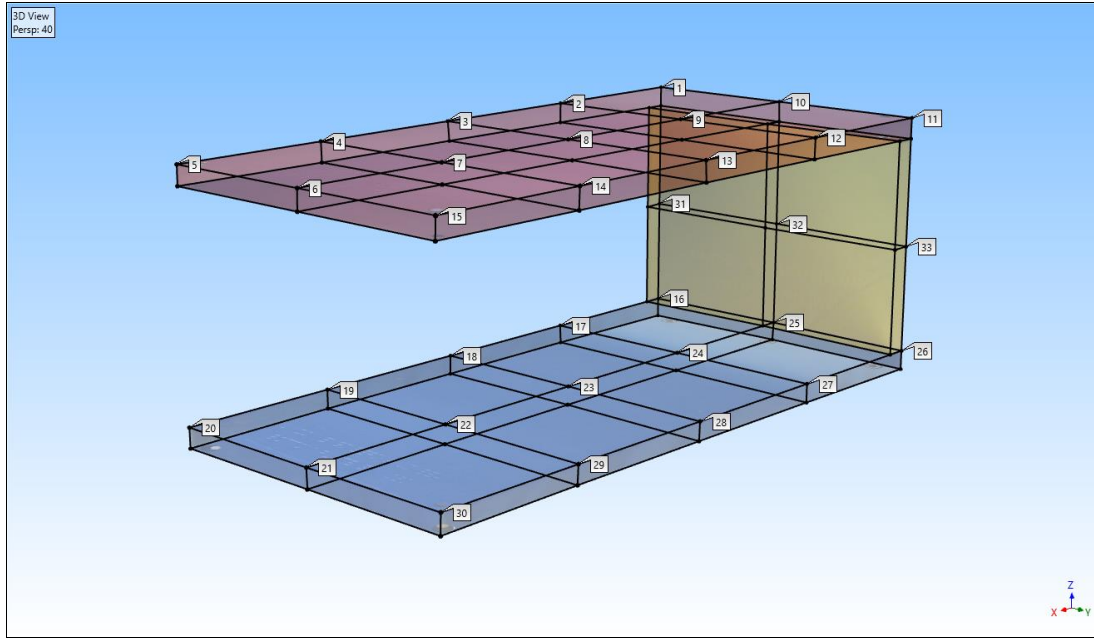


Types of FEA Objects used by SDM

IMPACT TEST OF THE JIM BEAM

To acquire a set of **FRFs**, the Jim Beam was impacted at one corner of the top plate. A tri-axial accelerometer was moved between impacts and attached to each of 33 different points on the top, bottom, & vertical plates of the beam structure, as shown below.

This provided **99 FRFs**, which preserve the dynamics between the **Input at DOF 15Z**, and **3D (X, Y, Z) Outputs at 33 Points**. By curve fitting the **FRFs**, **Residue** mode shapes for ten modes with **99 DOFs in each mode shape** are estimated from the **FRFs**. A **Modal Model** is then created by re-scaling the **Residue** mode shapes to **UMM** mode shapes starting with the driving point mode shape component (**15Z:15Z**) of each **Residue** mode shape.



Jim Beam Model Showing 33 Test Points.

STEP 1 - MODE SHAPES OF THE UNMODIFIED JIM BEAM

- **Press Hotkey 1 Mode Shapes of the Jim Beam**

When **Hotkey 1** is pressed, a **Modal Model** of the Jim Beam is obtained by curve fitting a set of **FRFs** for the Jim Beam, and re-scaling the **Residue** mode shapes estimated from curve fitting to **UMM** mode shapes.

Sweep animation is then begun through the mode shapes in the Shape Table **SHP: UMM Mode Shapes** displayed on the right side. Each shape is deflected using several cycles of sine dwell animation.

- **Press a Select Shape** button in **SHP: UMM Mode Shapes** to display its mode shape

From the animated display of each mode shape it is evident that the dominant motion of each mode shape is in the **vertical Z-direction**, except for the **165 Hz** mode shape. The **165 Hz** mode shape is a **torsional (twisting)** mode shapes of the back vertical plate.

The **165 Hz** mode shape has **dominant motion of the top & bottom plates in the horizontal plane**.

Select Shape	Frequency (or Time)	Damping	Units	Damping (%)
1	164.9	3.085	Hz	1.87
2	224.4	6.622	Hz	2.949
3	247.6	5.155	Hz	1.462
4	461.9	10.59	Hz	3.291
5	493.8	4.602	Hz	0.9339
6	635.2	14.23	Hz	2.242
7	1108	4.96	Hz	0.4476
8	1210	7.122	Hz	0.5883
9	1323	7.25	Hz	0.5481
10	1555	17.11	Hz	1.1

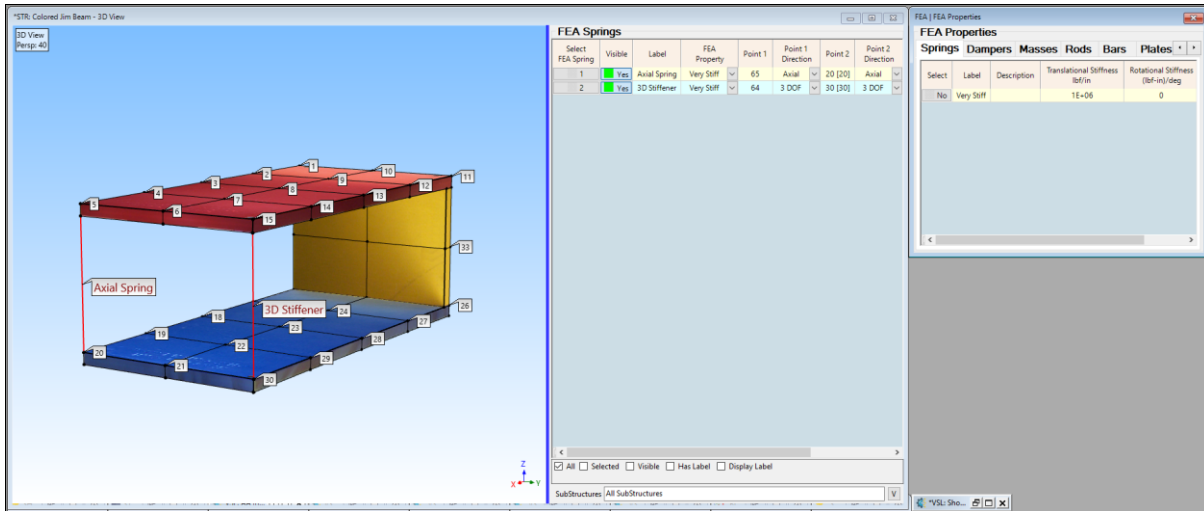
Select M#	DOFs	Units	Measurement Type	Label	Shape 1 Magnitude	Phase
MM1	1X	in/lbf-sec	UMM Mode Shape	Poly	4.327	10.81
MM2	1Y	in/lbf-sec	UMM Mode Shape	Poly	4.194	193.2
MM3	1Z	in/lbf-sec	UMM Mode Shape	Poly	5.724	193.5
MM4	2X	in/lbf-sec	UMM Mode Shape	Poly	4.021	4.709
MM5	2Y	in/lbf-sec	UMM Mode Shape	Poly	1.577	167.6
MM6	2Z	in/lbf-sec	UMM Mode Shape	Poly	8.332	192.2
MM7	3X	in/lbf-sec	UMM Mode Shape	Poly	3.431	2.768
MM8	3Y	in/lbf-sec	UMM Mode Shape	Poly	1.935	4.201
MM9	3Z	in/lbf-sec	UMM Mode Shape	Poly	8.231	190
MM10	4X	in/lbf-sec	UMM Mode Shape	Poly	3.996	7.278
MM11	4Y	in/lbf-sec	UMM Mode Shape	Poly	6.067	5.555
MM12	4Z	in/lbf-sec	UMM Mode Shape	Poly	8.359	185.1
MM13	5X	in/lbf-sec	UMM Mode Shape	Poly	3.911	8.037
MM14	5Y	in/lbf-sec	UMM Mode Shape	Poly	9.361	6.283
MM15	5Z	in/lbf-sec	UMM Mode Shape	Poly	9.389	192.7
MM16	6X	in/lbf-sec	UMM Mode Shape	Poly	0.1352	10.9
MM17	6Y	in/lbf-sec	UMM Mode Shape	Dolu	9.51	7.176

Deflection of the 165 Hz Jim Beam Mode Shape.

STEP 2 - SPRING & STIFFENER BETWEEN THE TOP & BOTTOM PLATES

- **Press Hotkey 2 Show the Axial Spring and 3D Stiffener**

Two **FEA Springs** have already been added to the **FEA Springs** spreadsheet on the right of the **vertical blue splitter bar**, as shown below



Two FEA Springs Between the Top & Bottom Plates.

The **Axial Spring** is connected between **Point 65 & Point 20** on the model

The **Axial Spring** provides stiffness in the **Axial direction** at both points

Point 20 also has a label [20]. Point 65 is the point on the bottom of the top plate. Point 65 has no label but it has an **M# Link** that uses the mode shape data from **Point [5]** above it.

SDM will use the mode shape data for **Point [5] and Point [20]** for its calculation.

3D Stiffener is connected between **Point 64 & Point 30** on the model

3D Stiffener will provide stiffness in **3 DOFs** at both end points

Point 30 has a label [30]. Point 64 is the point on the bottom of the top plate. Point 64 has no label but it has an **M# Link** that uses the mode shape data from **Point [15]** above it.

SDM will use the mode shape data for **Point [15] and Point [30]** for its calculation.

When used by **SDM**, each of these FEA Springs will add stiffness between the top & bottom plates. A spring property called **Very Stiff** has already been selected in the **FEA Properties** cell for each FEA Spring

A very large **Stiffness** has already been defined in the **FEA | Properties** box. **Very Stiff** → **1E+06 lbf/in**

COMPATIBLE ENGINEERING UNITS

To use **SDM**, the engineering units of the mode shapes in the Shape Table (**SHP: UMM Mode Shapes**) must be **compatible** with the units of the structural modification **FEA Objects** that are attached to the model.

The current engineering units for *each M#* in **SHP: UMM Mode Shapes** are (**in/lbf-sec**) as shown above. Those are compatible with the **force (lbf) & displacement (in)** units of the **Stiffness** in the **FEA | Properties** box.

CHANGING UNITS

To change engineering units from **English** to **Metric** units in **SHP: UMM Mode Shapes**,

- **Double click** on the **Units** column heading in the **M#s** spreadsheet of **SHP: UMM Mode Shapes**
- Enter "**m/N**" into the dialog box that opens
- **Click on Yes** in the next dialog box to re-scale the mode shapes to Metric units (**m/N-sec**)

To change engineering units from **English** to **Metric** units in the **FEA | Properties** box,

- Execute **File | MEscope Options** to open the **MEscope Options** box
- On the **Units** tab, select **Mass, Length, & Force** units to match the units in **SHP: UMM Mode Shapes**

If you change engineering units in the **STR** window, properties in the **FEA | Properties** dialog box **will be changed to the new units**.

The model is now ready to perform **SDM** calculations.

STEP 3 - AXIAL SPRING BETWEEN THE TOP & BOTTOM PLATES

- **Press Hotkey 3 SDM with the Axial Spring**

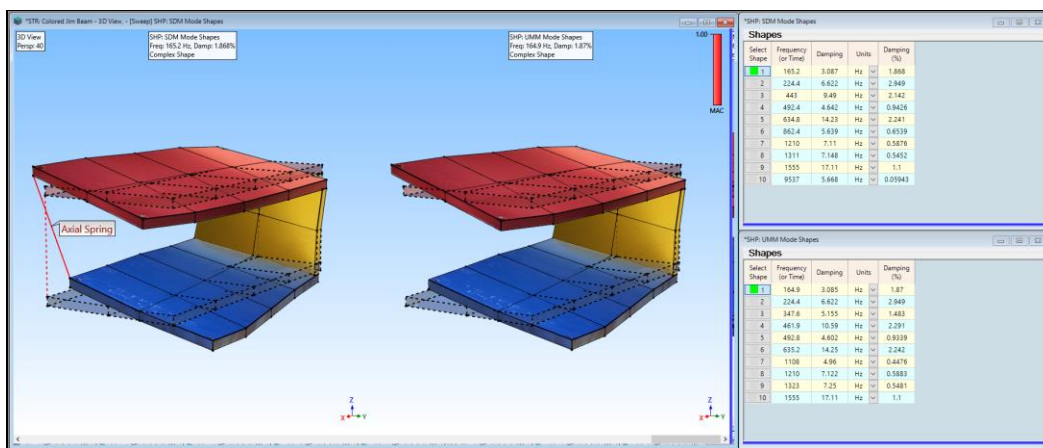
When **Hotkey 3 is pressed**, **SDM** will calculate the new modes of the Jim Beam with the **stiff Axial Spring** attached between the top & bottom plates, and save the new mode shapes in the Shape Table **SHP: SDM Mode Shapes**.

The Axial Spring only applies stiffness to the top & bottom plates along its own axis.

This becomes apparent when the new mode shapes are displayed in animation.

Sweep animation will begin through the mode shapes in **SHP: SDM Mode Shapes**, displaying each shape with **several cycles of sine dwell animation**. Each new mode shape is displayed side-by-side with its **closest-matching** mode shape from the mode shapes of the **unmodified structure** in **SHP: UMM Mode Shapes**.

Each **closest-matching** mode shape pair has a **Maximum MAC** value from among all the mode shapes in both Shape Tables.



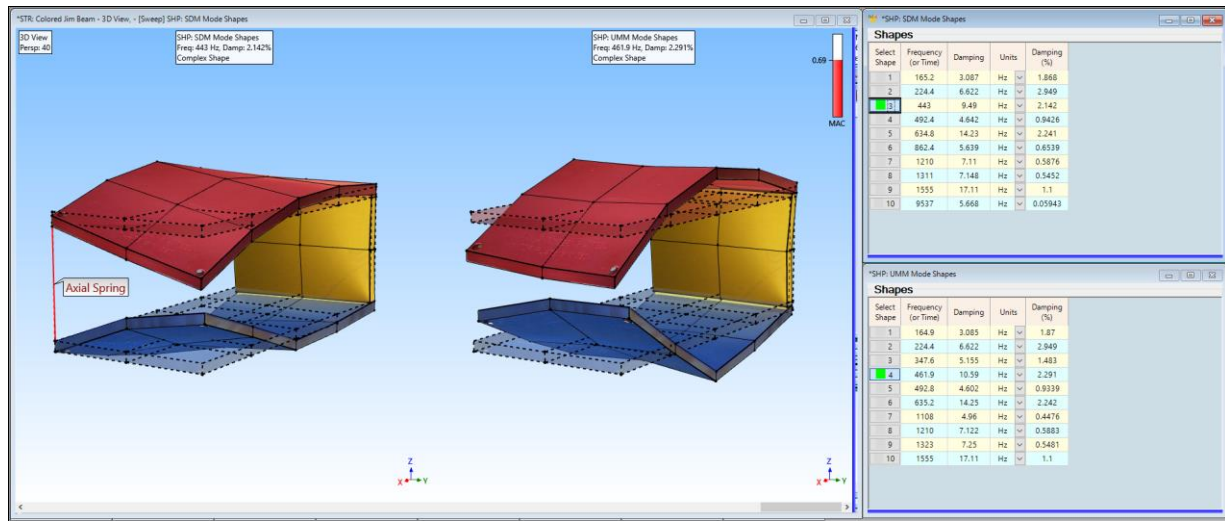
Closest-Matching Mode Shapes of Modified & Unmodified Jim Beam.

The mode shapes of **Shape 1 & Shape 2** in both Shape Tables are the same (**MAC → 1.00**) because those two mode shapes have **little or no relative motion along the axis of the FEA spring between the upper & lower plates**. The stiffener did not affect these two modes.

- **Click on Shape 3 (443 Hz) in SHP: SDM Mode Shapes**

This **new mode shape** clearly shows the effect of the stiffener. The **unmodified structure** had modes at **348 & 462 Hz**, both of which no longer exist in the modified structure.

MAC → 0.69 between this new mode shape and the **closest-matching 462 Hz** mode shape of the **unmodified structure** indicating that a new mode shape exists at **443 Hz**.



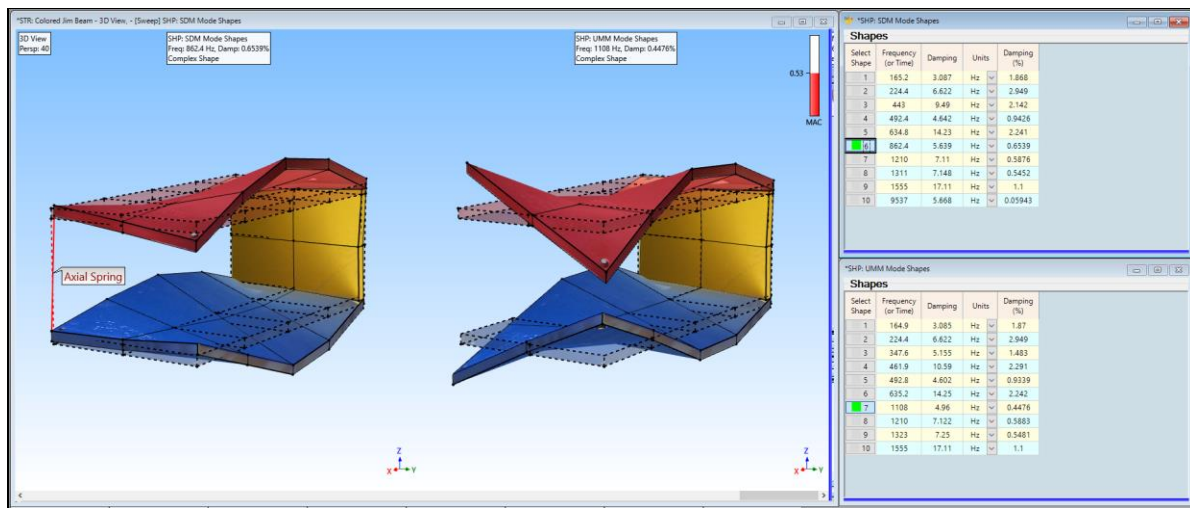
443 Hz Mode Shape Showing Influence of the Axial Spring.

- **Click on Shape 6 (862 Hz) in SHP: SDM Mode Shapes**

This **new mode shape** also clearly shows the effect of the stiffener.

MAC → 0.53 between this new mode shape and the **closest matching 1108 Hz** mode shape of the **unmodified structure** indicating that a new mode shape exists at **862 Hz**.

The remaining mode shapes each have a **high MAC value** with one of the modes of the **unmodified structure**, meaning that **those modes were not affected** by the Axial Spring.



862 Hz Mode Shape Showing Influence of the Axial Stiffener

TRUNCATED MODAL MODEL

The **Modal Model** that was used to model the dynamics of the *unmodified structure* had only 10 modes in it, yet it was assumed to represent the **entire dynamics of the unmodified structure**.

The real-world Jim Beam structure has more than 10 modes, ideally an **infinite number of modes**.

A **Modal Model** with only 10 modes in it is called a **truncated Modal Model** because the higher frequency modes of the real structure are not included in it.

When a **truncated Modal Model** is used by **SDM** to calculate the new modes of a *modified structure*, one or more of the highest frequency mode shapes in the solution are called **computational modes**. Computational modes have **unrealistic** mode shapes.

- **Click on Shape 10 (9550 Hz) in SHP: SDM Mode Shapes**

The animated display of **Shape 10 does not exhibit the effect of the Axial Spring**. It is clearly a computational mode.

A **truncated Modal Model** is **not a complete dynamic model** of the *unmodified structure*

The highest frequency modes in an **SDM** solution **typically have unrealistic mode shapes** and **much higher frequencies** than the rest of the mode shapes

Higher frequency modes in an **SDM** solution account for the **absence of the higher frequency modes** of the real-world structure

The higher frequency **SDM** modes **absorb the effects of the modification** that would **normally be absorbed by the modes not contained in the truncated Modal Model**

SDM still provides **useful solutions for the lower frequency modes**, even when a **truncated Modal Model** is used to model the dynamics of the *unmodified structure*.

STEP 4 - 3D STIFFENER BETWEEN THE TOP & BOTTOM PLATES

- **Press Hotkey 4 SDM with the 3D Stiffener**

When **Hotkey 4 is pressed** **SDM** will calculate the new modes of the Jim Beam with a **stiff 3D Stiffener** attached between the top & bottom plates, and save the new mode shapes in the Shape Table **SHP: SDM Mode Shapes**.

The 3D Stiffener applies stiffness in **all three directions (X, Y, Z)** at its end points.

The **UMM** mode shapes of the Jim Beam contain DOFs in **three directions (X, Y, Z)** at the end points of the 3D Stiffener, **SDM** will use the 3D mode shape data to calculate the new mode shapes.

Sweep animation will begin through the new modes in **SHP: SDM Mode Shapes**, displaying each shape with **several cycles of sine dwell animation**. Each new mode shape is displayed side-by-side with its **closest-matching** mode shape from among the modes of the *unmodified structure* in **SHP: UMM Mode Shapes**.

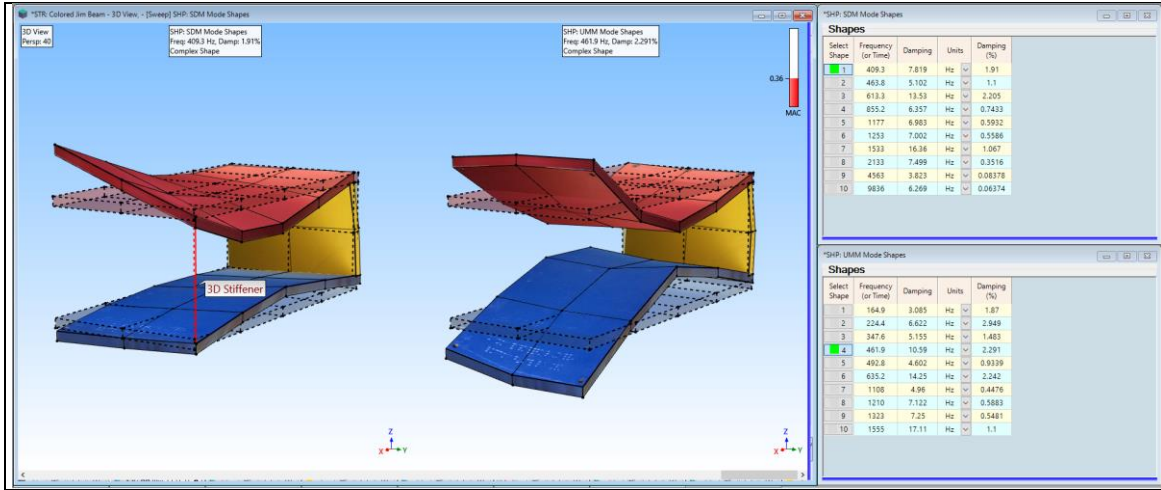
The **lowest frequency** mode shape of the *modified structure* is at **409 Hz**.

The **closest-matching** mode shape of the *unmodified structure* to the new **409 Hz** mode was the **462 Hz** mode shape, with **MAC → 0.36**.

The mode shapes of (**Shapes 3, 5, & 7**) have **MAC → 0.90**. They are the **closest-matching** shapes with those of the *unmodified Jim Beam*. Their frequencies also **closely match** the frequencies of the *unmodified structure*.

The remaining new modes have **MAC → less than 0.90**, meaning that **none of those new modes matches well** with one of the modes of the *unmodified structure*.

All modes of the unmodified structure were more heavily affected by the 3D Stiffener than by the Axial Spring.



409 Hz Mode Shape Showing Influence of the 3D Stiffener.

STEP 5 - REVIEW STEPS

To review the previous steps of this App Note,

- **Press Hotkey 5 Review Steps**