

# **VIBRANT** MEscope Application Note 29

# **Updating an FEA Model of an Aluminum Plate**

The steps in this Application Note can be carried out using any MEscope package that includes the VES-4600 Advanced Modal Analysis and VES-8000 Finite element Analysis options. Without these options, you can still carry out the steps in this App Note using the **AppNote29** project file. These steps might also require *a more recent release date* of MEscope.

# **APP NOTE 29 PROJECT FILE**

To retrieve the Project file for this App Note, **click here** to download **AppNote29.zip** •

This Project contains numbered Hotkeys & Scripts of commands for carrying out the steps of this App Note.

• Hold down the Ctrl key and click on a Hotkey to open its Script window

# STRUCTURAL DYNAMICS MODIFICATION (SDM

**SDM** has become a practical tool for improving the engineering designs of mechanical systems. It provides a very quick and inexpensive approach for investigating the effects of design modifications to a structure, thus eliminating the need for costly prototype fabrication and testing.

#### **MODAL MODEL**

SDM is unique in that it works directly with a modal model of the structure, either an Experimental Modal Analysis (EMA) modal model, a Finite Element Analysis (FEA) modal model, or a hybrid modal model consisting of both EMA & FEA mode shapes. EMA mode shapes are extracted from experimental data on a real-world test article. FEA mode shapes are extracted from a finite element computer model.

A modal model is a set of *properly scaled* mode shapes. SDM assumes that the mode shapes are scaled to Unit Modal Masses, called UMM mode shapes. A modal model preserves the mass & elastic properties of a structure, and it fully represents its dynamic properties.

# **DESIGN MODIFICATIONS**

Once the dynamic properties of an unmodified structure are defined in the form of its modal model, SDM can be used to predict the dynamic effects of certain kinds of mechanical design modifications to the structure. These modifications can be as simple as point mass, linear spring, or linear damper *additions to* or *removals from* the structure, or more complex modifications that are modeled using FEA elements such as RODS, BEAMS, PLATES (membranes) and SOLID ELEMENTS.

**SDM** solves an eigenvalue problem in modal space and is computationally more efficient and therefore faster than **FEA** which obtains mode shapes by solving an eigenvalue problem in physical space.

Another advantage is that **SDM** only requires the mode shape components of the unmodified structure for the DOFs (points & directions) where the modification elements are attached to the structure.



SDM Diagram

**SDM** is depicted in the diagram above.

# FEA MODEL UPDATING

Because of its computational speed, **SDM** can be used to quickly evaluate *thousands of potential modifications* to the physical properties of an **FEA** model. Although the **FEA** mode shapes of a structure may correlate well with its **EMA** mode shapes of a structure, the frequencies of the **FEA** mode shapes may differ significantly for the frequencies of the **EMA** resonances. Since modal frequencies are *very sensitive* to the physical properties of a structure, the difference between **FEA** & **EMA** modal frequencies can result from inaccurate physical properties in the **FEA** model.

In this example, two physical properties of the aluminum plate shown in the figure below will be updated to make its **FEA** mode shape frequencies *more closely match* its **EMA** mode shape frequencies. The two properties are the thickness and density of the aluminum material of the plate.

**SDM** will be used in **FEA Model Updating** to calculate the influence of *100's of different plate thickness & material density values* of the **FEA** model of the plate structure so that its modal frequencies are *more closely matched* with its **EMA** modal frequencies.

The dimensions of the plate are 20 inches (508 mm) by 25 inches (635 mm) by 3/8 inches (9.525 mm) thick.



Aluminum Plate Test Article

# **ROVING IMPACT MODAL TEST**

A roving impact modal test was conducted on the aluminum plate. The plate was tested while resting on bubble pack, which approximates free-free boundary conditions. The plate was impacted with an instrumented hammer at each point in a rectangular grid of 30 points which are numbered as shown below. A fixed reference accelerometer was attached near Point 5.

Thirty **FRFs** were calculated from the acquired impact time waveforms. The plate was impacted in the Z-direction, normal to its surface. Therefore, only Z-direction motion at each of the 30 points is defined by the **EMA** mode shapes that are extracted from the **FRFs** by curve fitting them.

The reference accelerometer can have been attached *anywhere on the surface*. The location of the reference accelerometer *will not influence the mode shapes* extracted from the **FRF** measurements. The mode shapes *only depend on each* **DOF** *where the plate was impacted* with the hammer.



Impact Test Points for Roving Impact Modal Test.

# **STEP 1 - CURVE FITTING THE FRFs**

# • *Press* Hotkey 1 EMA Plate Mode Shapes

When Hotkey 1 is *pressed*, EMA mode shapes for 14 modes are extracted from the FRFs. Each mode shape has 30 M#s, (with DOFs 1Z through 30Z). A curve fit on one of the FRFs is shown below.



Curve Fit of an Experimental FRF.



Animation of an EMA Mode Shape Side-by-Side with the Closest Matching ODS.

If you *press* Yes in the dialog that opens, sweep animation will begin through the EMA mode shapes in SHP: EMA Mode Shapes. Each mode shape is displayed side-by-side with the *closest matching* ODS at the Line cursor position in BLK: 30 Plate FRFs

• Press a Select Shape button in SHP: EMA Mode Shapes to display that mode shape and its closest matching ODS

The *closest matching* **ODS** has the **Maximum MAC** value with the currently selected **EMA** mode shape.

Notice that all the shape pairs have MAC  $\rightarrow$  1.0, indicating that each *closest matching* ODS is *co-linear* with each selected EMA mode shape.

# **STEP 2 - FEA MODE SHAPES OF THE PLATE**

An **FEA** model was constructed using *80 FEA plate (membrane) elements*. It is saved in the **STR: FEA Plate Model** file. The following properties of the aluminum material were selected from the **FEA Materials** dialog box, and the plate thickness was nominally chosen as **0.375 in. (9.525 mm)** 

Young's modulus of elasticity: 1E+07 lbf/in^2 (6.895E+04 N/mm^2)

Density: 0.101 lbm/in^3 (2.796E-06 kg/mm^3)

Poisson's Ratio: 0.33

Plate thickness: 0.375 in (9.525 mm)

To display the aluminum material properties,

• Open the **FEA** | **FEA** Materials dialog box.

FEA Materials       Select     Label     Description     Elasticity Ibf/in^2     Poisson's Ratio     Density Ibm/in^3       No     Carbon Steel     3E+07     0.3     0.283       No     Stainless Steel     2.8E+07     0.3     0.289       No     Gray Cast Iron     1.4E+07     0.26     0.264       No     Ductile Cast Iron     2.45E+07     0.3     0.256       No     Aluminum     1E+07     0.33     0.321
SelectLabelDescriptionElasticity lbf/in^2Poisson's RatioDensity lbm/in^3NoCarbon Steel3E+070.30.283NoStainless Steel2.8E+070.30.289NoGray Cast Iron1.4E+070.2640.264NoDuctile Cast Iron2.45E+070.30.256NoAluminum1E+070.330.0101NoCopper1.67E+070.330.321
No     Carbon Steel     3E+07     0.3     0.283       No     Stainless Steel     2.8E+07     0.3     0.289       No     Gray Cast Iron     1.4E+07     0.26     0.264       No     Ductile Cast Iron     2.45E+07     0.3     0.256       No     Aluminum     1E+07     0.33     0.101       No     Copper     1.67E+07     0.33     0.321
No     Stainless Steel     2.8E+07     0.3     0.289       No     Gray Cast Iron     1.4E+07     0.26     0.264       No     Ductile Cast Iron     2.45E+07     0.3     0.256       No     Aluminum     1E+07     0.33     0.101       No     Copper     1.67E+07     0.33     0.321
No     Gray Cast Iron     1.4E+07     0.26     0.264       No     Ductile Cast Iron     2.45E+07     0.3     0.256       No     Aluminum     1E+07     0.33     0.101       No     Copper     1.67E+07     0.33     0.321
No     Ductile Cast Iron     2.45E+07     0.3     0.256       No     Aluminum     1E+07     0.33     0.101       No     Copper     1.67E+07     0.33     0.321
No     Aluminum     1E+07     0.33     0.101       No     Copper     1.67E+07     0.33     0.321
No     Copper     1.67E+07     0.33     0.321
No. Constant 275-06 0.2 0.007
No Concrete 3.7E+06 0.2 0.087

To display the **FEA** plate thickness,

• Open the **FEA** | **FEA Properties** dialog and *click* on the **Plates** tab

FEA Properties     Springs   Dampers   Masses   Rods   Bars   Plates   Solids     Select   Label   Description   Material   Thickness in Multiplier   Multiplier     No   Plate 1   Aluminum v   0.375   1	🖳 FEA   FEA Properties											
Springs Dampers Masses Rods Bars Plates Solids   Select Label Description Material Thickness in Multiplier Stiffness Multiplier   No Plate 1 Aluminum 0.375 1	FEA Properties											
Select     Label     Description     Material     Thickness in     Stiffness Multiplier       No     Plate 1     Aluminum     0.375     1		Spring	IS E	Dar	npers	Ma	asses	Ro	ds	Bars	Plates	Solids
No Plate 1 Aluminum V 0.375 1		Select	Lab	el	Descripti	on	Mat	aterial		Thickness in	Stiffness Multiplier	
		No	Plate	e 1			Alumin	um	$\sim$	0.375	1	

# FEA PLATE ELEMENTS

The **FEA** model shown below has 99 points (or nodes) AND 80 **FEA** Quad Plate elements. The eigen-solution of **FEA** mode shapes will include *6 rigid body mode shapes* along with *flexible body mode shapes*. Each **FEA** mode shape will have *593 DOFs* (three translational & 3 rotational **DOFS** at each point).

The points (nodes) of the **FEA** model that *coincide* with the **EMA** test points have been given the *same point numbers* as the test points. This is required to calculate Modal Assurance Criterion (MAC) values using common **DOFs** between pairs of the **FEA** & **EMA** mode shapes.



The FEA mode shapes are UMM mode shapes, which is required by SDM for FEA Model Updating.

FEA Model with 80 FEA Quad Plate Elements

#### • Press Hotkey 2 FEA Plate Mode Shapes

When **Hotkey 2** is *pressed*, the **FEA** model of the plate is solved for its mode shapes, the **FEA** mode shapes are stored into **SHP: FEA Mode Shapes**, and a **sweep animation** of the **FEA** mode shapes is begun. Each **FEA** mode shape is displayed side-by-side with its *closest matching* **EMA** mode shape.

The *closest matching* EMA mode shape has the Maximum MAC value with each FEA mode shape.

All the mode shape pairs have **MAC** *close to* **1.0**. this indicates that each **FEA** mode shape is like its *closest matching* **EMA** mode shape with **Maximum MAC**.

• *Press* a Select Shape button in SHP: FEA Mode Shapes to display that mode shape and its *closest matching* EMA mode shape



Animation of an FEA Mode Shape Side-by-Side with Closest Matching EMA Mode Shape.

# **MODE SHAPE COMPARISON (MAC)**

The **Modal Assurance Criterion** (**MAC**) value between each **EMA** mode shape and its *closest matching flexible body* **FEA** mode shape is also displayed in the upper right corner of the side-by-side display of the mode shapes. The matching pairs of **FEA & EMA** mode shapes are listed in the table below.

The following *rules of thumb* are used with MAC,

MAC values → *between* 0 & 1

MAC = 1.0 → two shapes are co-linear (lie on the same straight line)

MAC >=  $0.9 \rightarrow$  two shapes *are similar* 

MAC < 0.9 → two shapes are linearly independent (do not lie on the same straight line)

The *worst-case pair* of closely matching mode shapes has a  $MAC \rightarrow 0.98$ . These high MAC values indicate a *very good correlation* between the EMA & FEA mode shapes using their *matching shape components* (DOFs 1Z through 30Z).

# MODAL FREQUENCY COMPARISON

The modal frequencies of the matching pairs of FEA & EMA mode shapes are listed in the table below.

Even though the **FEA** and **EMA** mode shapes are closely matched, each **EMA** modal frequency *is higher than* the frequency of its matching **FEA** mode.

These differences indicate that the stiffness of the real-world aluminum plate *is greater than* the stiffness of the **FEA** model. These frequency differences could be reduced by,

- Increasing the modulus of elasticity or reducing the density of the aluminum property of the FEA plates
- *Increasing the thickness* of the **FEA** plates

EMA Shape Number	EMA Frequency (Hz)	EMA Damping (Hz)	FEA Shape Number	FEA Frequency (Hz)	MAC
1	101.4	0.061	7	91.33	<mark>0.98</mark>
2	129.2	0.272	8	115.4	<mark>0.99</mark>
3	208.2	0.497	9	190.0	<mark>0.99</mark>
4	242.0	0.118	10	217.2	<mark>0.99</mark>
5	284.0	0.144	11	251.0	<mark>0.99</mark>
6	367.5	0.639	12	332.1	<mark>0.98</mark>
7	468.8	0.161	13	411.8	<mark>0.98</mark>
8	477.0	0.351	14	424.1	<mark>0.98</mark>
9	567.1	2.975	15	495.4	<mark>0.99</mark>
10	643.2	0.940	16	563.2	<mark>0.99</mark>
11	713.6	3.532	17	625.6	<mark>0.98</mark>
12	741.9	0.934	18	653.2	<mark>0.98</mark>
13	802.0	0.493	19	688.4	<mark>0.98</mark>
14	858.6	3.081	20	756.2	<mark>0.98</mark>

EMA Versus FEA Modal Frequencies & Mode Shape MAC

# **DIFFERENCE BETWEEN MODAL SENSITIVITY & FEA MODEL UPDATING**

In MEscope, **SDM** is used to provide solutions for both **Modal Sensitivity Analysis** and **FEA Model Updating**. But **SDM** is used differently by these two commands.

**FEA Model Updating** requires the *element properties of the unmodified* **FEA model**. **Modal Sensitivity Analysis** does not require the *element properties of the unmodified* **FEA model**.

# MODAL SENSITIVITY ANALYIS

To perform **Modal Sensitivity Analysis**, only a **modal model** of the *unmodified* **structure** and the **FEA** *modification elements are required*. The mass, stiffness and damping properties of the modification elements are converted into mass, stiffness, & damping modification matrices, which are then transformed into modal coordinates using the mode shapes of the *unmodified* structure.

The modification matrices in modal coordinates are then added to the modal matrices of the *unmodified* structure, and those equations are solved for the new modes of the *modified* structure.

# FEA MODEL UPDATING

To update the properties of an **FEA** model, **SDM** is used in a different way. First, the mass & stiffness properties of the *unmodified* **FEA** model *are subtracted from* the mass & stiffness properties of the *modified* **FEA** model. Then those differences are added to the modal matrices of the *unmodified* model.

# **STEP 3 - FEA MODEL UPDATING**

The physical properties used for the plate elements of the FEA model were,

#### Young's modulus of elasticity: 1E+07 lbf/in^2 (6.895E+04 N/mm^2)

Density: 0.101 lbm/in^3 (2.796E-06 kg/mm^3)

Poisson's Ratio: 0.33

#### Plate thickness: 0.375 in (9.525 mm)

The Plate is made from **6061-T651** aluminum. The correct density for that type of aluminum is **0.0975** lbm/in^3 (**2.966E-6** kg/mm^3. This is less than the density used in the FEA model. The Plate elements were assigned a *nominal thickness of* **0.375** in (**9.525** mm). Errors in either of these parameters could cause the FEA modal frequencies to be less than their corresponding EMA frequencies.

#### • Press Hotkey 3 FEA Model Updating

When Hotkey 3 is *pressed*, the FEA Model Updating window will open, as shown below.

# **UPPER SPREADSHEET**

The frequencies of the **FEA** mode shapes are listed in the first column of the *upper spreadsheet*. The modal frequency of each closely matched **EMA** mode shape (with the highest **MAC** value) is listed in the next column.

• Select mode pairs 7, 8, & 9 in the upper spreadsheet

# LOWER SPREADSHEET

The solution spaces for the **FEA** properties are listed in the *lower spreadsheet*. The solution space for each property is defined by three parameters, (**minimum**, **maximum** & **steps**).

FEA   FEA Model Updating														
Select Pair	FEA Frequency (Hz	El ) Freque	/IA hcy (Hz)		Targ Frequen	jet cy (Hz)	Includ MAC	e s Free	Solution quency (Hz)	Solutio Error	n	Solution MAC	^	
1	0	367.4 - MA	C: 0.2216	~	367	.4	No							
2	0	567.1 - MA	C: 0.2021	~	567	.1	No							
3	0	567.1 - MA	C: 0.2021	~	567	.1	No	,						
4	0	567.1 - MA	C: 0.2021	~	567	.1	No	,						
5	0.0001361	567.1 - MA	C: 0.2021	~	567	.1	No	,						
6	0.1562	208.1 - MA	0.07482	~	208	.1	No	,						
7	91.38	101.4 - MA	C: 0.9847	~	101	.4	No	,						
8	115.5	129.2 - MA	C: 0.9924	~	129	.2	No	,						
9	190.1	208.1 - MA	C: 0.9907	~	208	.1	No	,						
10	217.3	242 - MA	C: 0.995	~	24	2	No	,						
11	251.1	284 - MAG	: 0.9888	~	28	4	No	,						
12	332.3	367.4 - MA	C: 0.9848	~	367	.4	No	•						
13	412	468.8 - MA	C: 0.9751	~	468	.8	No	,						
14	424.3	477 - MAG	: 0.9857	~	47	7	No	,						
15	495.7	567.1 - MA	C: 0.9942	~	567	.1	No	,						
16	563.6	643.2 - MA	C: 0.9906	~	643	.2	No	,						
17	625.9	713.6 - MA	C: 0.9821	~	713	.6	No	,						
18	653.6	741.9 - MA	C: 0.9868	~	741	.9	No	,						
					1			_					Ť	-
Soluti	on Space													
Select Property	Property / Label	Property Type	Currer Value	nt :	Solution Value	Prope Unit	rty Pi s Mi	operty nimum	Property Maximum	Prope	erty is			
1	Plate 1	Thickness	0.375	;	0	in	(	0.375	0.5	10	÷			
2	Plate 1	Stiffness Multipl	er 1		0			0.9	1.1	10				
3	Aluminum	Elasticity	1E+0	7	0	lbf/in/	2 9	E+06	1.1E+07	10	÷			
4	Aluminum	Poisson's	0.33		0		(	).297	0.363	10	÷			
5	Aluminum	Density	0.101		0	lbm/in	^3	0.09	0.11	10	<b>A</b>			
Calcul	Calculate     Save Mode Shapes     Update Properties     Stop Calculation     Bar Charts     Spreadsheets     Close													

FEA Model Updating Before Calculating 100 Solutions

#### App Note 29

The solution space for the plate thickness is defined with 10 evenly spaced **Property Steps** between a **Property Minimum = 0.375** and a **Property Maximum = 0.50**. The solution space for the density is **defined with 10 evenly Property Steps between a Property Minimum = 0.90** and a **Property Maximum = 0.11. 100** solutions will be calculated with **SDM** using all combinations of values in the solution space of the **Thickness & Density** properties.

- Press the Select Property buttons for the Thickness and Density properties in the lower spreadsheet
- Press the Calculate button on the bottom of the FEA Model Updating window

After 100 solutions have been calculated, they will be ordered from best to worst, and the best solution will be displayed in the **FEA Model Updating** window, as shown below.

The best solution is the one with mode pairs 7, 8 & 9 closest in frequency to their target frequencies

The best solution is displayed when the scroll bar on the far right is at the top of its slider

The *best updated thickness* = 0.4167 in. which is greater than the nominal thickness (0.375) originally used

The *best updated density* = 0.1011 which is the *same as the density* chosen for aluminum

🖷 FEA   FEA Model Updating														
FEA-EMA Pairs														
Select Pair	FEA Frequency (H	EMA z) Frequenc	y (Hz)		Tar <u>o</u> Frequen	get cy (Hz)	Include MAC	Fre	Solution quency (Hz)	Solut Erre	tion or	Solution MAC	^	
1	0	367.45 - MAC:	0.22159	~	367.	45	No		80000.0	1		0.00453		
2	0	567.08 - MAC:	0.20206	~	567.	08	No		0.00009	1		0.20204		
3	0	567.08 - MAC:	0.19398	~	567.	08	No		0.00016	1		0.20204		
4	0	567.08 - MAC:	0.20178	~	567.	08	No		0.00081	1		0.20190		
5	0.00007	567.08 - MAC:	0.20370	~	567.	08	No		0.00182	1		0.00006		
6	0.15609	208.15 - MAC:	0.07482	~	208.	15	No		0.14808	0.999	929	0.07483		
7	91.331	101.44 - MAC:	0.98474	~	101.	44	No		101.46	0.0002	1849	0.98469		
8	115.4	129.17 - MAC:	0.99240	$\sim$	129.	17	No		128.2	0.0074	4939	0.99239		
9	189.99	208.15 - MAC:	0.99073	~	208.	15	No		211.05	0.013	925	0.99073		
10	217.18	242.02 - MAC:	0.99498	~	242.	02	No		241.25	0.0031	1682	0.99498		
11	250.96	283.96 - MAC:	0.98878	~	283.	96	No		278.77	0.018	264	0.98878		
12	332.13	367.45 - MAC:	0.98480	~	367.	45	No		368.83	0.0037	7662	0.98480		
13	411.8	468.77 - MAC:	0.97507	~	468.	77	No		457.36	0.024	339	0.97461		
14	424.11	477 - MAC: 0	98573	~	47	7	No		471.07	0.012	429	0.98540		
15	495.42	567.08 - MAC:	0.99425	~	567.	08	No		550.08	0.029	981	0.99427		
16	563.24	643.2 - MAC: (	0.99063	~	643	.2	No		625.37	0.027	718	0.99066		
17 625.59 713.61 - MAC: 0.98213			~	713.	61	No		694.42	0.026	898	0.98214	~	·	
Soluti	on Space													- 1
Select Property	Property Label	Property Type	Current Property		Solution Property	Proper Units	ty Pro Min	perty imum	Property Maximum	Prope Step	erty ps			
1	Plate 1	Thickness	0.375		0.41667	in	0	375	0.5	10	•			
2	Plate 1	Stiffness Multiplier	1		1			0.9	1.1	10	•			
3	Aluminum	Elasticity	1E+07		1E+07	lbf/in^	2 9E	+06	1.1E+07	10	•			
4	Aluminum	Poisson's	0.33		0.33		0	297	0.363	10	-			
5	Aluminum	Density	0.10111		0.10111	lbm/in/	<u>3</u> 0	.09	0.11	10	•			
Calcu	late Save	e Mode Upda napes Prope	ate rties	Ci	Stop alculation	В	ar Charts		Spreadsheets			Close		

FEA Model Updating After Calculating 100 Solutions

# • Scroll through the *first several solutions*

The first several solutions yield similar updated frequencies. *Any one of those solutions* could be used for updating the **FEA** model.

• Press the Save Mode Shapes button in the FEA Model Updating window

When the **Save Mode Shapes** button is *pressed*, **SDM** is used to calculate mode shapes using the currently displayed **Solution Properties** in the **FEA Model Updating** window.

# STEP 4 - SDM MODE SHAPES VERSUS EMA MODE SHAPES

#### • *Press* Hotkey 4 SDM vs. EMA Mode Shapes

When **Hotkey 4** is *pressed*, sweep animation through the mode shapes in **SHP: SDM Mode Shapes** will begin, and each **SDM** mode shape is displayed side-by-side with its *closest matching* **EMA** mode shape. The **MAC** value of each pair of mode shapes is also displayed in the *upper right corner* of the mode shapes display, and in the table below.



Animation of an SDM Mode Shape Side-by-Side with the Closest Matching EMA Mode Shape.

SDM Shape Number	SDM Frequency (Hz)	EMA Shape Number	EMA Frequency (Hz)	EMA Damping (Hz)	МАС
7	101.5	1	101.5	0.04487	<mark>0.98</mark>
8	128.2	2	129.1	0.264	<mark>0.99</mark>
9	211	3	208.1	0.4977	<mark>0.99</mark>
10	241.3	4	242.0	0.1089	<mark>0.99</mark>
11	278.8	5	284.0	0.1444	<mark>0.99</mark>
12	368.8	6	367.5	0.6455	<mark>0.98</mark>
13	457.4	7	468.7	0.1659	<mark>0.97</mark>
14	471.1	8	477.0	0.3509	<mark>0.99</mark>
15	550.1	9	567.1	2.979	<mark>0.99</mark>
16	625.4	10	643.2	0.9498	<mark>0.99</mark>
17	694.4	11	713.6	3.583	<mark>0.98</mark>
18	725.4	12	741.9	0.9449	<mark>0.99</mark>
19	764.3	13	802.0	0.4814	<mark>0.98</mark>
20	839.5	14	858.6	3.087	<mark>0.98</mark>

SDM Versus EMA Modal Frequencies & Mode Shape MAC

# STEP 5 - UPDATED FEA MODE SHAPES VERSUS SDM MODE SHAPES

In this step, the **FEA Model Updating** process is repeated, but this time the properties of the **FEA** model itself are updated and **FEA** mode shapes are calculated from the updated **FEA** model. The **FEA** mode shapes are then compared in side-byside animation with the **SDM** mode shapes that were calculated using the **updated FEA Properties** that were used by **SDM** in **Step 4**.

- Press Hotkey 3 FEA Model Updating again
- Press the Calculate button on the bottom of the FEA Model Updating window

When the calculation of 100 solutions has completed.

• *Press* the **Update Properties** button on the bottom of the **FEA Model Updating** window

The Thickness & Density properties are now updated in the FEA Properties & FEA Materials boxes.

• Press Hotkey 5 Updated FEA vs. SDM Mode Shapes

When **Hotkey 5** is *pressed*, **FEA** mode shapes are calculated from the FEA model with updated properties, and those mode shapes are compared in animation with the calculated with **SDM** and the plates with updated properties.

The comparison display will sweep through the mode shapes of the updated **FEA** model and display each mode shape sideby-side with the *closest matching* mode shape calculated by **SDM**. This side-by-side comparison is shown below.



Mode Shape of the Updated FEA Model Animated Side-by-Side with the Closest Matching SDM Mode Shape.

The table below lists the modal frequencies and **MAC** values between each mode shape of the updated FEA model and its *closest matching* **SDM** mode shape using the same updated plate **Thickness** and aluminum **Density** modifications.

Shape Number	Updated FEA Frequency (Hz)	SDM Frequency (Hz)	MAC
1	0	0.0001111	<mark>0.99</mark>
2	0	0.0001581	<b>1.00</b>
3	0	0.0001822	<mark>0.42</mark>
4	0	0.0008134	<mark>0.71</mark>
5	0	0.001824	<mark>0.90</mark>
6	0.1704	0.1481	1.00
7	101.5	101.5	1.00
8	128.2	128.2	1.00
9	211	211	1.00
10	241.3	241.3	1.00
11	278.8	278.8	1.00
12	368.8	368.8	1.00
13	457.4	457.4	1.00
14	471.1	471.1	1.00
15	550.1	550.1	1.00
16	625.4	625.4	1.00
17	694.4	694.4	1.00
18	725.4	725.4	1.00
19	764.3	764.3	1.00
20	839.5	839.5	1.00

Updated FEA Model Versus SDM Modal Frequencies & Mode Shape MAC.

# CONCLUSION

The table above shows a *perfect match* of the frequencies & MAC values between the flexible body mode shapes of the **updated FEA** model and those of the **SDM** calculation.

In this case, the **SDM** eigen-solution in modal space *perfectly matched* the eigen-solution in physical space calculated from the **FEA** model.

The eigen-solution in physical space used by the **FEA** solver yielded mode shapes that included *all the dynamic properties* of the plate, yet the accuracy of **SDM** was not impacted by using a *truncated modal model*,(only 20 of the modes of the plate).

Even though **SDM** started with a *truncated modal model* of the dynamics of the *unmodified plate*, the mode shapes calculated by **SDM** using the **modified plate properties** *closely compared* with the mode shapes of the **updated FEA** model.

# **STEP 6 - REVIEW STEPS**

To review the steps of this App Note,

• Press Hotkey 6 Review Steps